Third African School and Workshop

X-rays in Materials



January 23-28, 2012

Dakar

Basic crystallography



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DakarThird African SchoolJanuary 23-28, 2012and Workshop

X-rays in Materials

<u>Overview</u>

- X-rays, basic properties
- X-rays and materials structure
- Crystal lattices
- Some relevant crystal structures
- Crystal planes
- Reciprocal lattice

X-rays, basic properties

X-rays are electromagnetic waves





Propagating sinusoidal waves



3-D plane-waves: wave-vector





Electromagnetic spectrum



Interaction of x-rays with matter





X-rays and materials structure



Crystals

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Quartz crystal (SiO₂)

Macroscopic regularities (e.g. constancy of angles)

Classification of crystals



Regular packing of microscopic structural units R.J. Haüy (1743-1822)



X-ray diffraction from crystals





Crystallography

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William Henry Bragg (1862-1942)

Cambridge, 1912/13



Bragg spectrometer



William Lawrence Bragg (1890-1971)



Bravais lattice + basis







Macro and micro-crystals

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Monocrystalline silicon, \varnothing 13 cm





Cr, electron microscopy



Grain structure

Effects of temperature



Crystal lattices











Different choices of primitive vectors \vec{a}, \vec{b}



Primitive vectors (3D)

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3-D

$$\vec{R} = n_1 \vec{a} + n_2 \vec{b} + n_3 \vec{c}$$



Different choices of primitive vectors \vec{a} , \vec{b} , \vec{c}



Primitive cell = 1 lattice point



More than 1 lattice point per unit cell



Bravais lattices





Characterization of unit cells 2-D 3-D \vec{b} \vec{c} \vec{a} X \vec{b} γ B \vec{a}







Some relevant crystal structures

















Coordination number









Crystal planes

Crystal planes in 2D

























Planes and directions





Family of planes





Reciprocal lattice



Basic idea

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A) Family of planes \rightarrow wave-vector



Time periodicity



Space periodicity (1D)

















Reciprocal lattice and lattice planes

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For any family of lattice planes separated by a distance d there are reciprocal lattice vectors perpendicular to the planes, the shortest of which have a length $2\pi/d$.

For any reciprocal lattice vector R^* , there is a family of lattice planes normal to R^* and separated by a distance d, where $2\pi/d$ is the length of the shortest reciprocal lattice vector parallel to R^* .



- Plane waves and wavevector
- Crystalline and non-crystalline materials
- Crystal structure = Bravais lattice + basis
- Bravais lattices: primitive vectors, unit cells (primitive and conventional), classifications
- Crystal structures (sc, bcc, fcc, hcp ...)
- Crystal planes and Miller indices
- Reciprocal lattice

Snow crystals on an iced lake